

A STUDY ON QUEUING ISSUE IN TACTICALL ENVIRONMENT

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ABSTRACT

TactiCall MCI empowers direct correspondence from the individual mariner to central command. It encourages the proficient and quick trade of information and voice all through the whole system, using the best accessible data transmission paying little respect to the strategic condition. TactiCall MCI's stage independency will enable you to keep up your inheritance hardware while streamlining your operational effectiveness through, for example, specially appointed directing. TactiCall MCI will keep you associated with your very own powers, joint powers and partners while ideally abusing the accessible limit and improving your situational mindfulness and operational proficiency. This study represents the fact of Queuing issue consisting of different aspects like stages of service, service interruption, maintenance work and revamp process in TACTI CALL environment. This problem is well analyzed by means of supplementary variable method of Queuing approach. As a result we derive all the Queue performance measures of the above queuing issue. Numerical illustration and the graphical representation elaborate the explanation of the result at the end for the TactiCall environment queuing issue.

KEYWORDS

Service, Long vacation, Reneging, Short vacation, Service interruption, Repair, Delay.

1. INTRODUCTION

TactiCall MCI the executives interface utilizes a customer/server based HMI that is gotten to by verified T-MCI administrators utilizing standard HTTPS. T-MCI the executives administrators utilize this interface to control the switch and transmission frameworks. The administration HMI is actualized as a major aspect of the item and consequently requires no incorporation exertion. T-MCI likewise gives an immediate checking and control interface to applications (machine-to-machine). One of the essential employments of this interface is for T-MCI to give correspondence framework status data to applications on a sub-second reason for stream control purposes. This recreates the customary communication where an application is associated straightforwardly to the radio however without the burdens related with such stove channeling. T-MCI gives broad system checking data abilities by means of both the administration and application interfaces.

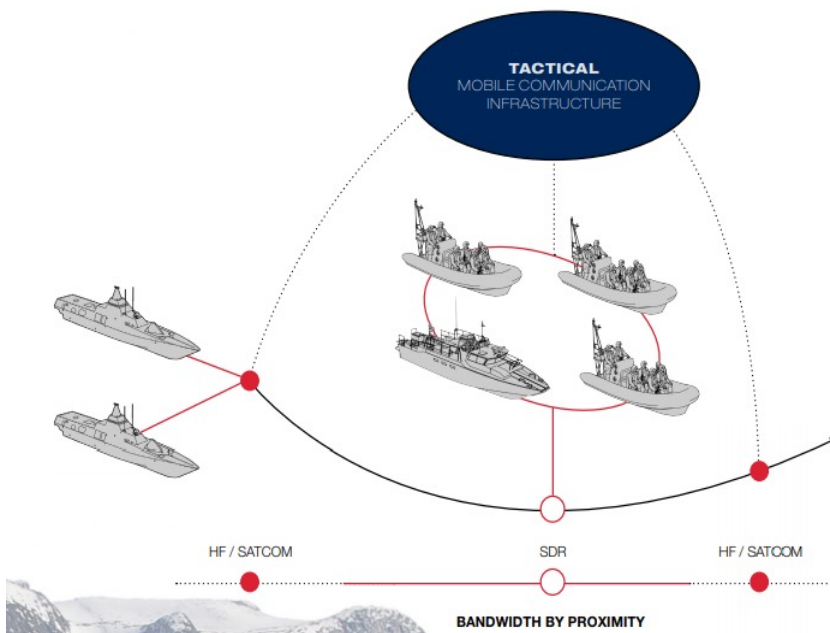
Artino, Folga, and Swan (2006) depicted another hypoxia worldview that consolidated the ROBD with strategic flight triggers. Majumdar (2005) gave the measurable estimation and calculation of correspondence parameters utilized in planning and advancing laser correspondence frameworks that were dependable under every single climate condition. Echols (2004) created specialized gauges that would take into account accomplishments of interoperability between worldwide strategic correspondence systems.

Chatterjee and Pal (1993) gave a diagram of the exceptional highlights and future patterns in satellite correspondence. Misra, Misra, and Tripathi (2013) talked about the progression of various applications viewpoint present and future in satellite correspondence. Erkan and Uzun (2004) depicted the essential highlights and client administrations of TASMUS and with the help of concurrent voice and information capacities, TASMUS intended to shape versatile, survivable, adaptable and secure system to help all the present and future correspondence prerequisites of the strategic leaders. Holmström, Rajamäki, and Hult (2011) accomplished the part hazards among administrators and correspondence channels; better directing and need capacities; considering security and interruption chances and including particularity.

Burkholder-Allen *et al.* (2009) displayed the Boutulism Questionnaire, which would help with the screening of setbacks, gave instructive and indicative signs to clinician and the

lay open, and made a layer of insurance for the social insurance framework. Suri *et al.* (2009) saw from a few strategic systems administration tests and shows the exercises gained from organization of the Mockets middleware to help strategic correspondences. Crainic (1988) surveys the fundamental issues with respect to the strategic arranging of cargo rail transportation and the important models tending to these issues. Maragathasundari and Sowmiyah (2015) made an investigation M/G/1 Queuing System with expanded excursion, administration interference; defer time and stages in fix. Strategic arranging models for inventory network the board analyzed by Swaminathan and Tayur (2003). Maragathasundari, Srinivasan, and Ranjitham (2014) researched clump landing queuing framework with two phases of administration.

1.1. TACTICALL MCI



Graphic 1. Tactical Mobile Communication Infrastructure.
Source: own elaboration.

TactiCall MCI is worked to help your operational necessities, keeping you associated with your system by conveying a hearty and secure voice and information correspondence arrangement. TactiCall MCI is a QoS - and asset mindful strategic switch that oversees

access to correspondence administrations (for example given by radios) for mixed media applications and arranged gadgets. TactiCall MCI's measured and versatile plan underpins inheritance joining in light of future development.

Utilize accessible heritage hardware, coordinate with IP systems administration and downplay relocation cost. Well-ordered delicate and equipment redesigns dependent on operational needs. Future-verification through simple well-ordered updates and extra usefulness Job based login. Evacuating stovepipes by presenting use of shared correspondence assets dependent on strategic conditions and current transmission prerequisites. Limit accumulation through organized data transfer capacity determination. Remote and adaptable administration of whole system through IP technology. Enhanced heartiness utilizing dynamic directing. Consistent incorporation of heterogeneous systems.

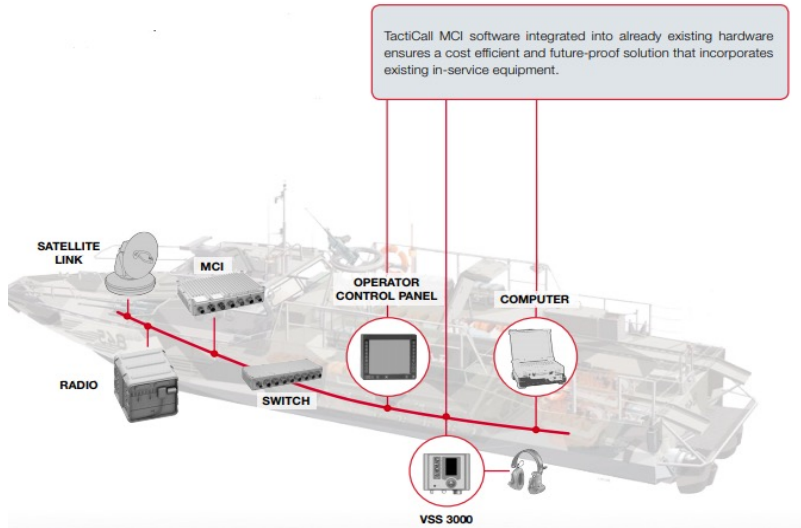
From the next section onwards various factors like service rendered in the tactical, different types of maintenance works, kinds of interruptions, delay in getting into the repair process and how the repair is carried out are explained in detail.

1.2. AD-HOC ROUTING

TactiCall MCI automatically chooses the highest possible bandwidth at all times – guaranteeing the best communication path available.

- 1) *Operational Ad-Hoc routing*
- 2) *Maximizing network performance.*
- 3) *Automatically optimizing bandwidth selection.*
- 4) *Enabling seamless data traffic.*

TactiCall MCI can be given as a virtual machine and facilitated on existing figuring equipment – implying that no new equipment is required. TactiCall MCI will guarantee stepwise incorporation and updates as per operational and mechanical prerequisites. TactiCall MCI programming coordinated into effectively existing equipment guarantees a cost productive and future-confirmation arrangement that consolidates existing in-administration gear.



Graphic 2. Tactical MCI software integrate.

Source: own elaboration.

1.3. SHORT VACATION (MINIMAL MAINTENANCE WORK)

Proactive MCI maintenance on the other hand, focuses on identifying and solving problems before they materialize.

During Short Vacation Types:

- 1) *Proactive Maintenance by the Engineer.*
- 2) *Cleaning Process.*
- 3) *First Line Service.*

One kind of protection upkeep is ordinarily performed by the designer who has been sent to a server in light of issue. While the designer is at the tactical server, the person in question will complete deterrent upkeep trying to avert future issues. Architects for the most part will check the best 10 realized deficiency conditions. Fault testing can be to a great extent manual procedure requiring a decent arrangement of time, anyway it's positively superior to no deterrent support by any means. Another way to deal with proactive support may be increasingly appealing to associations that desire to improve proficiency while bringing down operational expenses.

1.4. DURING LONG VACATION (MAXIMAL MAINTENANCE WORK)

- 1) *Second line Maintenance / Hardware testing*
- 2) *Software testing*

SECONDARY MAINTENANCE

This alludes to work which just tactical MCI seller's support faculty can do, for example, taking care of hardware breakdowns, parts trades, gear upkeep, and so forth. Experts adopt a proactive strategy to second Line Hardware Maintenance which incorporates the diagnosing of issues and the substitution of breaking down outer parts. By playing out various preventive support visits every year, they discover potential issues before the segment disappointment. Specialists supplant consumable parts, clean, grease up, adjust, and test the majority of the segments to guarantee appropriate usefulness. Experts are prepared to chip away at brands.

SOFTWARE TESTING

Designer needs to execute the accompanying Test Cases for maritime correspondence server created by the product engineer. And still, after all that it gathers more opportunity for correspondence server the mariners will become irritated and look for some other close-by exchange server. Consequently renegeing happens.

1.5. SERVER BREAKDOWN

Normally, when we state a server is down, what we mean is that the program that is intended to react to demands from the system isn't doing as such. That is our Tactical can't most likely react for the mariners in the proper time. There are various reasons that could occur, and every one of them requires an alternate arrangement. Here are a few models:

The ability to the MCI framework it keeps running on was cut. There are numerous reasons this could occur, including however not constrained to individuals pulling the wrong attachment while doing support, cleaning, and so forth. All things considered, you need to reestablish control.

The system association quit working. This could be a direct result of a physical link that got unplugged, or in light of the fact that some bit of system hardware fizzled. System gear can overheat. In some cases there are unobtrusive bugs in the product it runs that lone appear from time to time, and the system gear should be restarted. Now and again, some absolutely random framework utilizing a similar system can go haywire and flood the system with a lot of traffic, which could back off everything else and some of the time considerably trigger issues in the product or setup that aren't generally taken note.

The PC is associated with power and the system, however for reasons unknown it isn't quite. Perhaps the power was cut before, and the PC isn't designed to walk out on when the power is reestablished.

The PC is on; however the working framework isn't running. Generally this implies the working framework slammed, in which case the main thing you can do is more often than not to restart the machine, or that the working framework never stacked when the machine fueled up, which likely methods there is some kind of problem with the plate it is put away on.

1.6. REPAIR STAGE 1

1) The simplest solution is often the best

For instance, does the MCI server have control, or did somebody accidentally unplug the power rope? In the event that the machine clearly has control, however there doesn't appear to be any system availability, verify whether the Ethernet or fiber link has been unintentionally unplugged.

a) If basic troubleshooting doesn't work:

Since we've checked the majority of our links and other fringe gadgets, endeavor to ping the gadget from inside the LAN. Luckily, the ping order is general, so this ought to be clear paying little respect to the stage being used. In the event that the mariner can ping the server from inside the LAN, take a stab at pinging the server from outside of the LAN. Doing this will go far in deciding whether the issue is at the steering and exchanging level, as opposed

to at the server level. Additionally, if our Web server is virtualized, take a stab at pinging the IP address of the physical machine itself. This will assist us with furthering segregate the issue. In the event that we can't ping the server by any stretch of the imagination, and we've certainly checked the system association, it's an ideal opportunity to go further.

b) Delay: Nope, the Web server is still down:

We've checked the peripheral cables. The sailors've attempted to ping the box, and still don't have network access to the server. Fortunately you have basically disengaged the issue to either the physical machine or the working framework. Presently we understood that the whole programming arrangement .After finishing the real fix work, the server will go for the optional phase of fix that is to refreshing the working framework. That being said it accumulates more opportunity for correspondence server the mariners will become upset and scan for some other close-by substitute server. Consequently renegeing happens.

1.7. STAGE 2

Updates for working frameworks are discharging every now and again. Remaining over these updates can be motivating. This is the reason we use modernized fix the executives instruments and have checking set up to alarm us when a framework is obsolete. In the event that we are refreshing our server physically (or not under any condition), we may miss significant security refreshes. Programmers regularly filter for defenselessly frameworks inside hours of an issue being uncovered. So quick reaction is vital. After this whole programming upgrade, the mariner can use the tactical MCI uninterruptedly.

2. METHODOLOGY OF SOLVING THE ABOVE TACTI CALL ENVIRONMENTAL QUEUING ISSUE

The above characterized Queuing issue is disentangled by using the supplementary variable technique. For every one of the organization time, remain by server escape time and fix time valuable variables are used. Unwavering state line gauge dispersal and the different execution measure are settled. Numeral outline legitimizes the model and the graphical depiction gives a sensible picture about the decisions to be taken before the startup of the organization. To deteriorate the issue of clog in the TACTI CALL make benefits, an

obvious endorsement is rendered toward the end, by strategies for looking at the numerical results and graphical examination of the model.

2.1. STEPS INVOLVED IN THE USAGE OF SUPPLEMENTARY VARIABLE METHOD

First we frame the governing equations for the queuing problem involved in tactical environment in section by using the parameters like service rendered, short vacation, long vacation, system break down, delay in getting into repair process and stages of repair process.

As a second step, we process out the initial boundary conditions of the problem defined.

Next by the usage of various supplementary variables, we derive the probability generating function of the queue size of the tactical queuing problem. In continuation, length of the queue, number of customers (works to be carried out) in the system, waiting time of the customers in the queue as well as in the system are derived.

All those derivations are justified by means of numerical illustration and graphical portrayal. Based on that, investigation have been made in the numerical study and the analysis is carried out in the analysis report. Having a deep study on the analysis, one can get the idea of minimizing the service interruption in the tactical environment or to avoid in getting into break down of the system. Moreover system maintenance work is required whether for shorter duration or longer duration could be predicted. This study helps to carry out the various factors in tactical issue in an accurate manner. This leads to the length of the queue to be minimal in the system. Utilization factor would be made to a maximal. Tactical system works to a maximal level.

2.2. GOVERNING EQUATIONS OF THE MODEL

By means of birth and death process of Queuing study, we first frame the governing equations of the tactical issue:

$$\frac{d}{dx}M_n(x) + (\lambda + \mu(x) + \beta)M_n(x) = \lambda \sum_{j=1}^n d_j M_{n-j}(x). \quad (1)$$

$$\frac{d}{dx}M_0(x) + (\lambda + \mu(x) + \beta)M_0(x) = 0. \quad (2)$$

$$\frac{d}{dx} V_n^{(L)}(x) + (\lambda + \mu_L(x))V_n^{(L)}(x) = \lambda \sum_{j=1}^n d_j V_{n-j}^{(L)}(x). \quad (3)$$

$$\frac{d}{dx} V_0^{(L)}(x) + (\lambda + \mu_L(x))V_0^{(L)}(x) = 0. \quad (4)$$

$$\frac{d}{dx} V_n^{(S)}(x) + (\lambda + \mu_S(x))V_n^{(S)}(x) = \lambda \sum_{j=1}^n d_j V_{n-j}^{(S)}(x). \quad (5)$$

$$\frac{d}{dx} V_0^{(S)}(x) + (\lambda + \mu_S(x))V_0^{(S)}(x) = 0. \quad (6)$$

$$\frac{d}{dx} R_n^{(1)}(x) + (\lambda + \mu_r^{(1)}(x))R_n^{(1)}(x) = \lambda \sum_{j=1}^n d_j R_{n-j}^{(1)}(x). \quad (7)$$

$$\frac{d}{dx} R_0^{(1)}(x) + (\lambda + \mu_r^{(1)}(x))R_0^{(1)}(x) = 0. \quad (8)$$

$$\frac{d}{dx} D_n(x) + (\lambda + \eta(x) + \xi)D_n(x) = \lambda \sum_{j=1}^n d_j D_{n-j}(x) + \xi D_{n+1} \quad (9)$$

$$\frac{d}{dx} D_0(x) + (\lambda + \eta(x) + \xi)D_0(x) = 0. \quad (10)$$

$$\frac{d}{dx} R_n^{(2)}(x) + (\lambda + \mu_r^{(2)}(x))R_n^{(2)}(x) = \lambda \sum_{j=1}^n d_j R_{n-j}^{(2)}(x). \quad (11)$$

$$\frac{d}{dx} R_0^{(2)}(x) + (\lambda + \mu_r^{(2)}(x))R_0^{(2)}(x) = 0. \quad (12)$$

$$\lambda Q = \int_0^\infty M_0(x)\mu(x)dx + \int_0^\infty V_0^{(L)}(x)\mu_L(x)dx + \int_0^\infty V_0^{(S)}(x)\mu_S(x)dx + \int_0^\infty R_0^{(2)}(x)\mu_r^{(2)}(x)dx. \quad (13)$$

2.3. BOUNDARY CONDITIONS

The following boundary conditions are used to solve the above equations:

$$M_n(0) = \int_0^\infty M_{n+1}(x)\mu(x)dx + \int_0^\infty V_{n+1}^{(L)}(x)\mu_L(x)dx + \int_0^\infty V_{n+1}^{(S)}(x)\mu_S(x)dx + \int_0^\infty R_{n+1}^{(2)}(x)\mu_r^{(2)}(x)dx. \quad (14)$$

$$V_n^{(L)}(0) = a \int_0^\infty M_n(x)\mu(x)dx. \quad (15)$$

$$V_n^{(S)}(0) = b \int_0^\infty M_n(x)\mu(x)dx. \quad (16)$$

$$R_n^{(1)}(0) = \beta \int_0^\infty M_n(x). \quad (17)$$

$$D_n(0) = \int_0^\infty R_n^{(1)}(x)\mu_r^{(1)}(x)dx. \quad (18)$$

$$R_n^{(2)}(0) = \int_0^\infty D_n(x)\eta(x)dx. \quad (19)$$

2.4. DISTRIBUTION OF THE LINE LENGTH

Solving of equations from (1) - (12), multiply (1) by z^n and sum over n from 1 to ∞ and add it to (2) resulting the following equation:

$$\frac{d}{dx}M(x, z) + (\lambda - \lambda D(z) + \mu(x) + \beta)M(x, z) = 0. \quad (20)$$

Similarly,

$$\frac{d}{dx}V^{(L)}(x, z) + (\lambda - \lambda D(z) + \mu_L(x))V^{(L)}(x, z) = 0. \quad (21)$$

$$\frac{d}{dx}V^{(S)}(x, z) + (\lambda - \lambda D(z) + \mu_S(x))V^{(S)}(x, z) = 0. \quad (22)$$

$$\frac{d}{dx}R^{(1)}(x, z) + (\lambda - \lambda D(z) + \mu_r^{(1)}(x))R^{(1)}(x, z) = 0. \quad (23)$$

$$\frac{d}{dx}D(x, z) + \left(\lambda - \lambda D(z) + \xi - \frac{\xi}{z}\right)D(x, z) = 0. \quad (24)$$

$$\frac{d}{dx}R^{(2)}(x, z) + (\lambda - \lambda D(z) + \mu_r^{(2)}(x))R^{(2)}(x, z) = 0. \quad (25)$$

Applying the same for boundary conditions: Solving of equations from (1) - (12), multiply (1) by z^n and sum over n from 1 to ∞ and add it to (2) resulting the following equation:

Applying the same for boundary conditions:

$$zM(0, z) = \int_0^\infty M(x, z)\mu(x)dx + \int_0^\infty V^{(L)}(x, z)\mu_L(x)dx + \int_0^\infty V^{(S)}(x, z)\mu_S(x)dx + \int_0^\infty R^{(2)}(x, z)\mu_r^{(2)}(x) + \lambda(D(z) - 1)Q. \quad (26)$$

$$V^{(L)}(0, z) = a \int_0^\infty M(x, z)\mu(x)dx. \quad (27)$$

$$V^{(S)}(0, z) = b \int_0^\infty M(x, z)\mu(x)dx. \quad (28)$$

$$R^{(1)}(0, z) = \beta zM(z). \quad (29)$$

$$D(0, z) = \int_0^\infty R^{(1)}(x, z)\mu_r^{(1)}(x)dx. \quad (30)$$

$$R^{(2)}(0, z) = \int_0^\infty D(x, z)\eta(x)dx. \quad (31)$$

Now Integrating (20) from 0 to, it gives

$$M(x, z) = M(0, z)e^{-(\lambda - \lambda D(z)) - \int_0^\infty \mu(t)dt} \quad (32)$$

Integrating the above by parts, we get

$$M(x, z) = M(0, z) \left[\frac{1 - \bar{E}(a_1)}{a_1} \right], a_1 = \lambda - \lambda D(z) + \beta \tag{33}$$

Where $\bar{E}(a_1) = \int_0^\infty e^{-(\lambda - \lambda D(z) + \beta)x} dE(x)$ is the Laplace Stieltje’s transform of the service time. Again multiplying (32) by $\mu(x)$ and integrating, we get

$$\int_0^\infty M(x, z) \mu(x) dx = M(0, z) \bar{E}_1(a_1) \tag{34}$$

Similarly

$$V^{(L)}(z) = V^{(L)}(0, z) \left[\frac{1 - \bar{E}_2(a_2)}{a_2} \right], a_2 = \lambda - \lambda D(z) = aM(0, z) \bar{E}_1(a_1) \left[\frac{1 - \bar{E}_2(a_2)}{a_2} \right] \tag{35}$$

$$\int_0^\infty V^{(L)}(x, z) \mu_L(x) dx = V^{(L)}(0, z) \bar{E}_2(a_2) = aM(0, z) \bar{E}_1(a_1) \bar{E}_2(a_2). \tag{36}$$

$$V^{(S)}(z) = V^{(S)}(0, z) \left[\frac{1 - \bar{E}_3(a_2)}{a_2} \right] = bM(0, z) \bar{E}_1(a_1) \left[\frac{1 - \bar{E}_3(a_2)}{a_2} \right]. \tag{37}$$

$$\int_0^\infty V^{(S)}(x, z) \mu_S(x) dx = bM(0, z) \bar{E}_1(a_1) \bar{E}_3(a_2). \tag{38}$$

$$R^{(1)}(z) = R^{(1)}(0, z) \left[\frac{1 - \bar{E}_4(a_2)}{a_2} \right] = \beta z M(0, z) \left[\frac{1 - \bar{E}_1(a_1)}{a_1} \right] \left[\frac{1 - \bar{E}_4(a_2)}{a_2} \right]. \tag{39}$$

$$\int_0^\infty R^{(1)}(x, z) \mu_r^{(1)}(x) dx = \beta z M(0, z) \left[\frac{1 - \bar{E}_1(a_1)}{a_1} \right] \bar{E}_4(a_2). \tag{40}$$

$$D(z) = D(0, z) \left[\frac{1 - \bar{E}_5(a_3)}{a_3} \right], \text{ where } a_3 = \lambda - \lambda D(z) + \xi - \frac{\xi}{z} = \beta z M(0, z) \left[\frac{1 - \bar{E}_1(a_1)}{a_1} \right] \bar{E}_4(a_2) \left[\frac{1 - \bar{E}_5(a_3)}{a_3} \right]. \tag{41}$$

$$\int_0^\infty D(x, z) \eta(x) dx = \beta z M(0, z) \left[\frac{1 - \bar{E}_1(a_1)}{a_1} \right] \bar{E}_4(a_2) \bar{E}_5(a_3) \tag{42}$$

$$R^{(2)}(z) = R^{(2)}(0, z) \left[\frac{1 - \bar{E}_6(a_2)}{a_2} \right] = \beta z M(0, z) \left[\frac{1 - \bar{E}_1(a_1)}{a_1} \right] \left[\frac{1 - \bar{E}_6(a_2)}{a_2} \right] \bar{E}_4(a_2) \bar{E}_5(a_3). \tag{43}$$

$$\int_0^\infty R^{(2)}(x, z)\mu_r^{(2)}(x)dx = \beta z M(0, z) \left[\frac{1-\bar{E}_1(a_1)}{a_1} \right] \bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3). \tag{44}$$

Substituting (34), (36), (38), (44) in (26), we get:

$$M(0, z) = \frac{\lambda(D(z)-1)Q}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{45}$$

Using the above (33), (35), (37), (39) (41) and (43) becomes,

$$M(z) = \frac{\lambda(D(z)-1)Q\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{46}$$

$$V^{(L)}(z) = \frac{-\lambda Q a [1-\bar{E}_2(a_2)]\bar{E}_1(a_1)}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{47}$$

$$V^{(S)}(z) = \frac{-\lambda Q b \bar{E}_1(a_1)[1-\bar{E}_3(a_2)]}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{48}$$

$$R^{(1)}(z) = \frac{-\beta z \lambda Q \left[\frac{1-\bar{E}_1(a_1)}{a_1}\right][1-\bar{E}_4(a_2)]}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{49}$$

$$R^{(2)}(z) = \frac{-\beta z \lambda Q \left[\frac{1-\bar{E}_1(a_1)}{a_1}\right][1-\bar{E}_6(a_2)]\bar{E}_4(a_2)\bar{E}_5(a_3)}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{50}$$

$$D(z) = \frac{\beta z \lambda Q [D(z)-1] \left[\frac{1-\bar{E}_1(a_1)}{a_1}\right] \bar{E}_4(a_2) \left[\frac{1-\bar{E}_5(a_3)}{a_3}\right]}{z-\bar{E}_1(a_1)(\bar{E}_2(a_2)+\bar{E}_3(a_2)(a+b))-\beta z\bar{E}_6(a_2)\bar{E}_4(a_2)\bar{E}_5(a_3)\left[\frac{1-\bar{E}_1(a_1)}{a_1}\right]}. \tag{51}$$

3. RESULTS

3.1. PROBABILITY GENERATING FUNCTION OF THE QUEUE SIZE

To find the probability making limit of the line gauge paying little mind to the state of the structure. Let $W_q(z)$ be the probability generating function of the queue length no matter what the state of the system is

$$(i.e) W_q(z) = M(z) + V^{(L)}(z) + V^{(S)}(z) + R^{(1)}(z) + R^{(2)}(z) + D(z)$$

Then adding:

(46) – (51), we get:

$$\begin{aligned}
 & \lambda(D(z)-1)Q\left[\frac{1-\overline{E}_1(a_1)}{a_1}\right]-\lambda Qa[1-\overline{E}_2(a_2)]\overline{E}_1(a_1)- \\
 & \quad \lambda Qb\overline{E}_1(a_1)[1-\overline{E}_3(a_2)] \\
 & -\beta z\lambda Q\left[\frac{1-\overline{E}_1(a_1)}{a_1}\right][1-\overline{E}_4(a_2)]-\beta z\lambda Q\left[\frac{1-\overline{E}_1(a_1)}{a_1}\right] \\
 & \quad [1-\overline{E}_6(a_2)]\overline{E}_4(a_2)\overline{E}_5(a_3) \\
 W_q(z) = & \frac{\beta z\lambda Q[D(z)-1]\left[\frac{1-\overline{E}_1(a_1)}{a_1}\right]\overline{E}_4(a_2)\left[\frac{1-\overline{E}_5(a_3)}{a_3}\right]}{z-\overline{E}_1(a_1)(\overline{E}_2(a_2)+\overline{E}_3(a_2)(a+b))-} \\
 & \quad \beta z\overline{E}_6(a_2)\overline{E}_4(a_2)\overline{E}_5(a_3) \\
 & \quad \left[\frac{1-\overline{E}_1(a_1)}{a_1}\right]}
 \end{aligned} \tag{52}$$

The idle time Q is determined by using the normalization condition:

$$W_q(1)+Q=1$$

Using L'Hopital's rule, we get:

$$\lim_{z \rightarrow 1} W_q(z) = \frac{N'(1)}{D'(1)}$$

Also $Q = \frac{D'(1)}{D'(1)+N'(1)}$

From Q , the utilization factor ρ can be determined.

3.2. SYSTEM QUEUE EXECUTION PROCEDURES

Let L_q a chance to demonstrate the reliable state typical number of customers in the line.

By then:

$$L_q = \frac{d}{dz} W_q(z) \Big|_{z=1} = \frac{d}{dz} \left\{ \frac{N(z)}{D(z)} \right\} \Big|_{z=1}$$

Where $N(z)$ and $D(z)$ are the numerator and denominator of (52).

Since $W_q(z) = \frac{0}{0}$ at $z=1$, we utilize two-fold separation and get:

$$L_q = \lim_{z \rightarrow 1} \frac{d}{dz} W_q(z) = \frac{D'(1)N''(1) - D''(1)N'(1)}{2(D'(1))^2}. \tag{53}$$

Where primes mean subordinates with respect to z and after a course of action of logarithmic enhancement, we get length of the queue L_q closed frame.

$$D'(1) = 1 + 2\lambda(a + b)\overline{E_1}'(\beta) - (a + b)\lambda(E(B_2) + E(B_3)) - \beta \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) [1 - \overline{E_1}'(\beta) + \lambda E(B_4) + E(B_5)(-\lambda + \xi) + \lambda E(B_6)]. \tag{54}$$

$$N'(1) = \lambda \left\{ \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) (\beta E(B_5)) + \lambda(E(B_3) + E(B_2))\overline{E_1}(\beta)(a + b) \right\}. \tag{55}$$

$$N''(1) = \lambda \left\{ \lambda [E(B_2) + E(B_3)] \left[-\lambda \overline{E_1}'(\beta) + \beta \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) (E(B_6) + E(B_4)) \right] + \overline{E_1}'(\beta) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) (\beta E(B_5)) + \overline{E_1}'(\beta) + \overline{E_1}'(\beta) (\beta E(B_5)) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) [\beta E(B_5) + \lambda \beta E(B_4) E(B_5) + \beta(\lambda - \xi) E(B_5^2)] \right\}$$

$$\left\{ \lambda [E(B_2) + E(B_3)] \left[-\lambda \overline{E_1}'(\beta) + \beta \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) (E(B_6) + E(B_4)) \right] + \overline{E_1}'(\beta) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) (\beta E(B_5)) + \overline{E_1}'(\beta) + \overline{E_1}'(\beta) (\beta E(B_5)) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) [\beta E(B_5) + \lambda \beta E(B_4) E(B_5) + \beta(\lambda - \xi) E(B_5^2)] \right\}. \tag{56}$$

$$D''(1) = -2\lambda^2 \overline{E_1}''(\beta)(a + b) + \overline{E_1}'(\beta)(a + b)\lambda^2(E(B_2) + E(B_5)) + (a + b)\lambda^2 \overline{E_1}'(\beta)(E(B_2) + E(B_3)) - (a + b)\overline{E_1}(\beta)\lambda^2(E(B_2^2) + E(B_3^2)) - \beta \left[\left(-\overline{E_1}'(\beta)\right) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) \lambda [E(B_4) + E(B_5) + E(B_6)] \right] - \beta \left[-\overline{E_1}'(\beta) - \overline{E_1}'(\beta)\lambda [E(B_4) + E(B_5) + E(B_6)] + \lambda \overline{E_1}''(\beta) \right] - \beta \left[-\overline{E_1}'(\beta)\lambda E(B_4) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) \lambda E(B_4) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) [\lambda^2 E(B_4^2) + \lambda^2 E(B_6) E(B_4) + \lambda E(B_4) E(B_5)(-\lambda + \xi)] \right] - \beta \left[\left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) \lambda E(B_6) - \lambda \overline{E_1}'(\beta) E(B_6) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) [-\lambda^2 E(B_4) + \lambda^2 E(B_6^2) + \lambda E(B_5)(-\lambda + \xi)] \right] - \beta \left[\left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) E(B_5)(\lambda - \xi) + \left(\frac{1 - \overline{E_1}(\beta)}{\beta}\right) [\lambda E(B_4) E(B_5)(\lambda - \xi) + \lambda E(B_6) E(B_5)(\lambda - \xi) + (-\lambda + \xi)^2 E(B_5^2)] + \overline{E_1}(\beta) E(B_5)(-\lambda + \xi) \right]. \tag{57}$$

Substituting for $N^{\circ}(1), N^{\circ\circ}(1), D^{\circ}(1), D^{\circ\circ}(1)$ from (54) – (57) in (53), we obtain L_q in closed form.

Further the mean waiting time of a customer in the queue as well as in the system and the number of customers waiting in the system can be found using Little’s formula:

$$W_q = \frac{L_q}{\lambda}, W = \frac{L}{\lambda}, L = L_q + \rho$$

3.3. NUMERICAL JUSTIFICATION OF THE MODEL

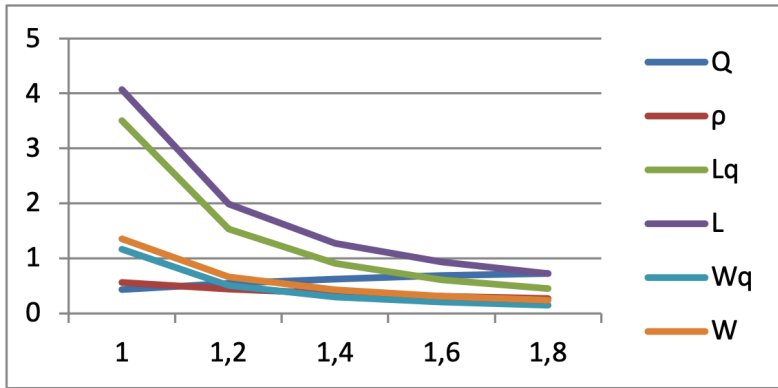
Assume that service time follows exponential distribution in particular and based on this condition, the numerical justification is elaborated below. The values are collected accordingly:

$$\begin{aligned} \mu &= 2.8, \mu_L = 3.6, \mu_S = 4.5, \mu_r^{(1)} = 3.5, \mu_r^{(2)} = 2, \eta = 3, \xi = 2.5, \beta = 3, \xi = 1, a = 0.6, b \\ &= 0.4\overline{E}_1'(\beta) = \frac{-\beta}{(\mu + \beta)^2}, E(B_2) = \frac{1}{\mu_L}, E(B_3) = \frac{1}{\mu_S}, E(B_4) = \frac{1}{\mu_r^{(1)}}, E(B_5) \\ &= \frac{1}{\eta}, E(B_6) = \frac{1}{\mu_r^{(2)}}, \overline{E}_1(\beta) = \frac{\mu}{\mu + \beta}, E(B_2^2) = \frac{2}{\mu_L^2}, E(B_5^2) = \frac{2}{\eta^2}, E(B_6^2) \\ &= \frac{2}{(\mu_r^{(2)})^2}, E(B_4^2) = \frac{2}{(\mu_r^{(1)})^2}, E(B_5^2) = \frac{2}{\mu_S^2} \end{aligned}$$

Table 1. Effect Of Change In ξ : $\xi=1,1.2,1.4,1.6,1.8$.

| Q | ρ | L_q | W_q | L | W |
|--------|--------|--------|--------|--------|--------|
| 0.4354 | 0.5646 | 3.5076 | 1.1692 | 4.0722 | 1.3574 |
| 0.5516 | 0.4484 | 1.5393 | 0.5131 | 1.9877 | 0.6626 |
| 0.6296 | 0.3704 | 0.9113 | 0.3038 | 1.2817 | 0.4272 |
| 0.6856 | 0.3144 | 0.6175 | 0.2058 | 0.9319 | 0.3106 |
| 0.7277 | 0.2723 | 0.4534 | 0.1511 | 0.7257 | 0.2419 |

Source: own elaboration.

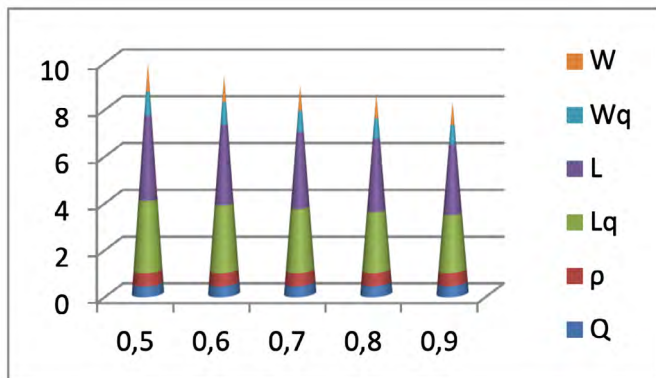


Graphic 3. Effect of change in ξ .
Source: own elaboration.

Table 2. Effect Of Change In a : a=0.5,0.6,0.7,0.8,0.9.

| Q | ρ | Lq | Wq | L | W |
|--------|--------|--------|--------|--------|--------|
| 0.4582 | 0.5418 | 3.0381 | 1.0127 | 3.5799 | 1.1933 |
| 0.4600 | 0.5400 | 2.8510 | 0.9503 | 3.3910 | 1.1303 |
| 0.4615 | 0.5385 | 2.6931 | 0.8971 | 3.2298 | 1.0766 |
| 0.4629 | 0.5371 | 2.5532 | 0.8511 | 3.0903 | 1.0301 |
| 0.4641 | 0.5359 | 2.4327 | 0.8109 | 2.9686 | 0.9895 |

Source: own elaboration.



Graphic 4. Effect of change in a.
Source: own elaboration.

4. DISCUSSIONS

All the values in the table are as expected. In Table 1, probability of considering the concept of renegeing takes place. Due to impatience, customers leave the system after joining the queue. This concept is defined as renegeing as explained earlier. Hence in this tactical issue increase in renegeing makes the work lessen to be carried out in tactical problem. Therefore length of the queue gets diminished. Number of customers in the system gets lessen too. This leads to the waiting time of the customers in the queue as well as in the system to get reduced. All these measures are gotten only due to the increase in the renegeing concept. This has to be avoided by the way of reducing the time factor of delay process. Hence whenever service interruption occurs, the system has to be introduced into the renegeing process immediately. Hence the server can render its service without any delay and it leads to keeps away from Renegeing.

Table 2 indicates the concept of increase in getting the probability of long vacation. So maximal maintenance work can be carried out in the system. Hence the increase in probability of long vacation, (the process of maintenance work time) makes the system to run faster than the earlier and hence the performance measures of the system get reduced. Maintenance work is the unavoidable feature in the concept of Queuing problem.

5. CONCLUSIONS

In nature of TACTI CALL, Queuing issue comprising of administration, short get-away, long excursion, administration interference, fix process, phases of fix process happen. Here we had an itemized examination on various kinds of excursions and administration break in the framework. What's more, in this lining framework, framework doesn't get onto fix process right away. It concedes a deferral between the administration separate and the procedure of fix. Additionally, here fix process is completed in two phases. Get-away procedure assumes a significant job in this Queuing procedure of correspondence study. The issue is very much explained by advantageous variable strategy and the essential execution measures are determined. Numerical investigation of the application delineates the Queuing approach towards the issue by and large. This introduction acknowledges noticeable work in social occasion units, correspondence structure, and development crossing centers, framework

planning, etc. Benefits of this queuing procedure is reducing the time for work delay. It helps to give the service to customers at right time.

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